

Result Summary - Overall

Moment Connection - Beam to Column

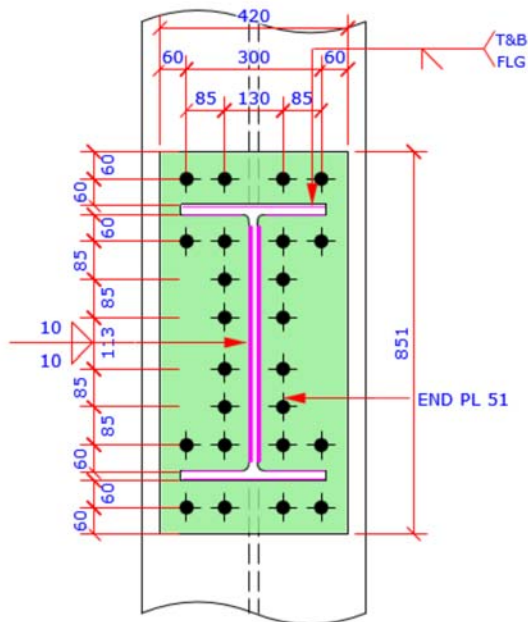
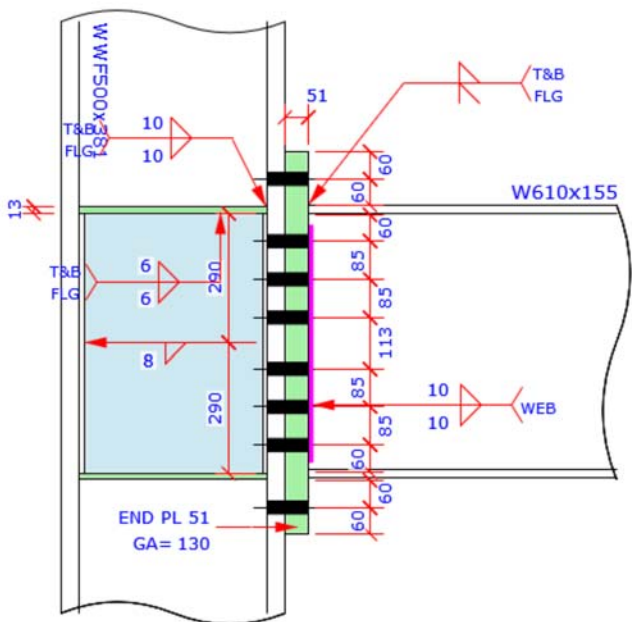
Code=AISC 360-10 LRFD

<b>Result Summary - Overall</b>	geometries & weld limitations = <b>PASS</b>	limit states max ratio = <b>0.83</b>	<b>PASS</b>
<b>Right Beam to Column</b>	geometries & weld limitations = <b>PASS</b>	limit states max ratio = <b>0.83</b>	<b>PASS</b>

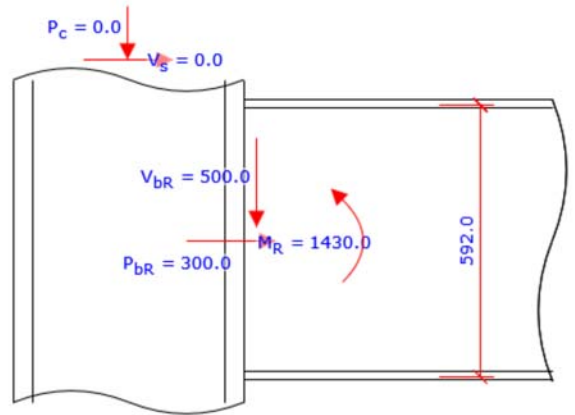
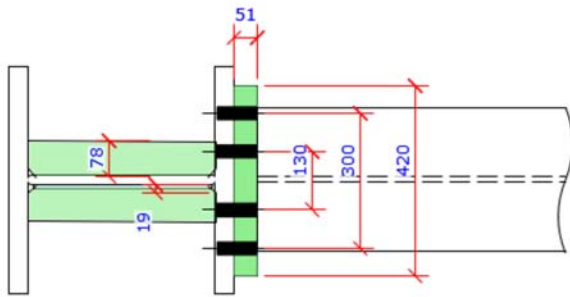
Sketch

Moment Connection - Beam to Column

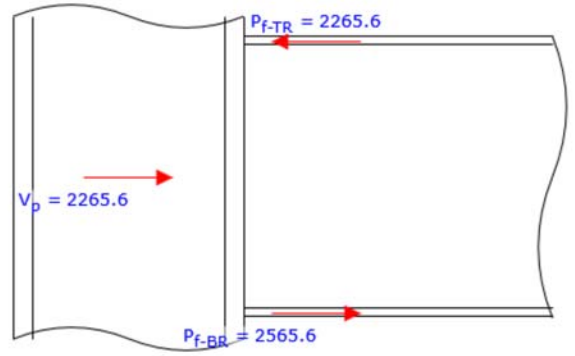
Code=AISC 360-10 LRFD



Right Side Beam



Design Load



Beam Flange Force & Panel Zone Shear  $V_p$

### Members & Components Summary

Member	Moment Connection	Code=AISC 360-10 LRFD
<b>Column Section</b>		
WWF500x381	$d = 500.0$ [mm]	$b_f = 500.0$ [mm]
	$t_f = 40.0$ [mm]	$t_w = 20.0$ [mm]
	$k_{des} = 51.0$ [mm]	$k_{det} = 51.0$ [mm]
	$k_1 = 0.0$ [mm]	$A = 48600$ [mm <sup>2</sup> ]
	$S_x = 9010.0$ [10 <sup>3</sup> mm <sup>3</sup> ]	$Z_x = 10100.0$ [10 <sup>3</sup> mm <sup>3</sup> ]
Steel Grade A992	$F_y = 344.8$ [MPa]	$F_u = 448.2$ [MPa]
<b>Right Side Beam Section</b>		
W610x155	$d = 611.0$ [mm]	$b_f = 324.0$ [mm]
	$t_f = 19.0$ [mm]	$t_w = 12.7$ [mm]
	$k_{des} = 41.0$ [mm]	$k_{det} = 41.0$ [mm]
	$k_1 = 27.0$ [mm]	$A = 19700$ [mm <sup>2</sup> ]
	$S_x = 4220.0$ [10 <sup>3</sup> mm <sup>3</sup> ]	$Z_x = 4730.0$ [10 <sup>3</sup> mm <sup>3</sup> ]
Steel Grade A992	$F_y = 344.8$ [MPa]	$F_u = 448.2$ [MPa]

### Beam Flange Force Calc

#### Beam Flange Force - Right Side Beam

Beam section	$d_b = 24.055$ [in]	$t_{fb} = 0.748$ [in]
Flange force moment arm	$d_m = d_b - t_{fb}$	$= 23.307$ [in]
User input load	axial $P_{bR} = -67.44$ [kips]	moment $M_R = 1054.73$ [kip-ft]
	in tension	
Beam flange force - top	$P_{f-TR} = P_{bR} / 2 + M_R / d_m$	$= 509.32$ [kips]
Beam flange force - bottom	$P_{f-BR} = P_{bR} / 2 - M_R / d_m$	$= -576.77$ [kips]

#### Panel Zone Shear Force Calc

Column story shear	$V_s =$ from user input	$= 0.00$ [kips]
Panel zone shear force	$V_p = P_{f-TR} - P_{f-TL} - V_s$	$= 509.32$ [kips]

Right Beam to Column      MC Connection      Code=AISC 360-10 LRFD

### Result Summary

geometries & weld limitations = **PASS**

limit states max ratio = **0.83** **PASS**

Geometry Restriction Checks			PASS
<b>Min Bolt Edge Distance - Column Flange</b>			
Bolt diameter	$d_b =$	= 1.250 [in]	
Min edge distance allowed	$L_{e-min} =$	= 1.625 [in]	AISC 14 <sup>th</sup> Table J3.4
Min edge distance in Column Flange	$L_e =$	= 3.937 [in]	
		> $L_{e-min}$	OK
<b>Min Bolt Spacing - End Plate</b>			
Bolt diameter	$d_b =$	= 1.250 [in]	
Min bolt spacing allowed	$L_{s-min} = 2.667 d_b$	= 3.333 [in]	AISC 14 <sup>th</sup> J3.3
Min Bolt spacing in End Plate	$L_s =$	= 3.346 [in]	
		> $L_{s-min}$	OK
<b>Min Bolt Edge Distance - End Plate</b>			
Bolt diameter	$d_b =$	= 1.250 [in]	
Min edge distance allowed	$L_{e-min} =$	= 1.625 [in]	AISC 14 <sup>th</sup> Table J3.4
Min edge distance in End Plate	$L_e =$	= 2.362 [in]	
		> $L_{e-min}$	OK
<b>Max Bolt Edge Distance - End Plate</b>			
Connecting plate thickness	$t_p =$	= 2.000 [in]	
Max edge distance allowed	$L_{e-max} = \min ( 12t , 6" )$	= 6.000 [in]	AISC 14 <sup>th</sup> J3.5
Max edge distance in End Plate	$L_e =$	= 2.362 [in]	
		< $L_{e-max}$	OK
<b>Beam Web Fillet Weld Limitation</b>			PASS
<b>Min Fillet Weld Size</b>			
Thinner part joined thickness	$t =$	= 0.500 [in]	
Min fillet weld size allowed	$w_{min} =$	= 0.188 [in]	AISC 14 <sup>th</sup> Table J2.4
Fillet weld size provided	$w =$	= 0.394 [in]	
		> $w_{min}$	OK
<b>Min Fillet Weld Length</b>			
Fillet weld size provided	$w =$	= 0.394 [in]	
Min fillet weld length allowed	$L_{min} = 4 \times w$	= 1.575 [in]	AISC 14 <sup>th</sup> J2.2b
Min fillet weld length	$L = 0.5 d_b - k_b$	= 10.414 [in]	
		> $L_{min}$	OK
<b>Min Beam Web to End Plate Fillet Weld Size</b>			
Beam web to end-plate fillet weld in the tension-bolt region to develop the yield strength of the beam web			AISC DG4 Page 9 Item 7
Shear resistance factor-LRFD	$\phi_v = 0.90$		AISC 14 <sup>th</sup> G1
Fillet weld shear strength	$\phi R_{n-w} =$	= 1.392 [kip/in]	AISC 14 <sup>th</sup> Eq 8-2a
Fillet weld strength $\phi R_{n-w} \times 1.5 \times 2$ to account for 90° load angle when it's in tension and double fillet			
Min double fillet weld size to match beam web yield strength	$D_{min} = \phi_v F_{yb} t_{wb} / ( \phi R_{n-w} \times 1.5 \times 2 )$	= 5.388 [1/16 "]	
Fillet weld size provided	$D =$	= 6.299 [1/16 "]	
		> $D_{min}$	OK

## Verify AISC DG4 Bolt No Prying Assumption

AISC DG4 Is Used

## Bolt Moment Strength (No Prying)

	bolt grade = A325-N	$F_t = 90.0$ [ksi]	AISC 14 <sup>th</sup> Table J3.2
	bolt dia $d_b = 1.250$ [in]	bolt area $A_b = 1.227$ [in <sup>2</sup> ]	
Bolt nominal tensile strength	$P_t = F_t A_b$	$= 110.45$ [kips]	AISC 14 <sup>th</sup> Eq J3-1
Tension bolt moment arm	$h_0 = 26.043$ [in]	$h_1 = 20.571$ [in]	
	$h_2 = 17.225$ [in]	$h_3 = 13.879$ [in]	

The following bolt moment without prying action for 12 bolts MRE 1/3-4W/2W bolt pattern is taken from Table 3-12 in Virginia Tech Report to MBMA, Developing and Validating New Bolted End-Plate Moment Connection Configurations July 2015 by Nonish Jain, Matthew Eatherton and Thomas Murray. Thomas Murray is the author of both AISC DG4 and DG16.

Bolt moment strength (no prying)	$M_{np} = 2 P_t (2 h_0 + 2 h_1 + h_2 + h_3)$	$= 2288.68$ [kip-ft]	
Bolt resistance factor-LRFD	$\phi = 0.75$		AISC 14 <sup>th</sup> Eq J3-1
	$\phi M_{np} =$	$= 1716.51$ [kip-ft]	

## End Plate Bending Strength

End plate width	$b_{plate} = 16.535$ [in]	thickness $t_p = 2.000$ [in]	
Beam flange width	$b_{fb} = 12.756$ [in]		
Effective end plate width	$b_p = \min (b_{plate}, b_{fb} + 1")$	$= 13.756$ [in]	AISC DG4 Page 9 item 5
End plate yield strength	$F_{yp} = 50.0$ [ksi]		

The following end plate yield line for 12 bolts MRE 1/3-4W/2W bolt pattern is taken from Table 3-12 in Virginia Tech Report to MBMA, Developing and Validating New Bolted End-Plate Moment Connection Configurations July 2015 by Nonish Jain, Matthew Eatherton and Thomas Murray. Thomas Murray is the author of both AISC DG4 and DG16.

formulas for calculating yield-line parameters

$$s = \frac{1}{2} \sqrt{b_p g} \quad \text{use } p_{fi} = s \quad \text{when } p_{fi} > s$$

$$Y_p = \frac{b_p}{2} \left[ \frac{h_0}{p_{fo}} + \frac{h_1}{p_{fi}} + \frac{h_3}{s} - 1 \right] + \frac{2}{g} \left[ h_1 (p_{fi} + 1.5 p_b) + h_3 (s + 0.5 p_b) \right] + \frac{g}{2}$$

Tension bolt moment arm	$h_0 = 26.043$ [in]	$h_1 = 20.571$ [in]	
	$h_2 = 17.225$ [in]	$h_3 = 13.879$ [in]	
	$g = 5.118$ [in]	$p_b = 3.346$ [in]	
	$p_{fi} = 2.362$ [in]	$p_{fo} = 2.362$ [in]	
	$s = 4.195$ [in]	$Y_p = 245.33$ [in]	
Flexure resistance factor-LRFD	$\phi_b = 0.90$		AISC 14 <sup>th</sup> F1 (1)
End plate bending strength	$\phi_b M_{pl} = \phi_b F_{yp} t_p^2 Y_p$	$= 3680.00$ [kip-ft]	
Check thick end plate condition	$\phi_b M_{pl} \geq 1.11 \times \phi M_{np}$		AISC DG4 Eq 3.33
	ratio = <b>0.52</b> thick plate		

## Column Flange Bending Strength

The column flange yield line for MRE 1/3 bolt pattern is taken from Table 8.13 of Virginia Tech Emmet Sumner's PhD thesis - Unified Design of Extended End-Plate Moment Connections Subject to Cyclic Loading June, 2003. This thesis was approved by Thomas M. Murray who is the author of AISC DG4 and DG16.

formulas for calculating yield-line parameters

<b>Bolt Moment Strength (No Prying)</b>		ratio = 576.77 / 883.77 = <b>0.65</b>		<b>PASS</b>
	bolt grade = A325-N	$F_t = 90.0$ [ksi]		AISC 14 <sup>th</sup> Table J3.2
	bolt dia $d_b = 1.250$ [in]	bolt area $A_b = 1.227$ [in <sup>2</sup> ]		
Bolt nominal tensile strength	$P_t = F_t A_b$	= 110.45 [kips]		AISC 14 <sup>th</sup> Eq J3-1
Tension bolt moment arm	$h_0 = 26.043$ [in] $h_2 = 17.225$ [in]	$h_1 = 20.571$ [in] $h_3 = 13.879$ [in]		
Flange force moment arm	$d_m = d_b - t_{fb}$	= 23.307 [in]		
Flange force required in tension	$P_{uf,t} = P_u / 2 - M_u / d_m$	= <b>576.77</b> [kips]		
Flange force resistance by bolt	$F_n = 2 P_t (2h_0 + 2h_1 + h_2 + h_3) / d_m$	= 1178.36 [kips]		
Bolt resistance factor-LRFD	$\phi = 0.75$			AISC 14 <sup>th</sup> Eq J3-1
	$\phi F_n =$	= <b>883.77</b> [kips]		AISC DG4 Eq 3.7
	ratio = <b>0.65</b>	> $P_{uf,t}$	<b>OK</b>	
<b>Bolt Shear Strength</b>		ratio = 112.41 / 596.41 = <b>0.19</b>		<b>PASS</b>
Bolt shear stress	bolt grade = A325-N	$F_{nv} = 54.0$ [ksi]		AISC 14 <sup>th</sup> Table J3.2
	bolt dia $d_b = 1.250$ [in]	bolt area $A_b = 1.227$ [in <sup>2</sup> ]		
Number of bolt carried shear	$n_s = 12.0$	shear plane $m = 1$		
Required shear strength	$V_u =$	= <b>112.41</b> [kips]		
Bolt shear strength	$R_n = F_{nv} A_b n_s m C_{ec}$	= 795.22 [kips]		AISC 14 <sup>th</sup> Eq J3-1
Bolt resistance factor-LRFD	$\phi = 0.75$			AISC 14 <sup>th</sup> Eq J3-1
	$\phi R_n =$	= <b>596.41</b> [kips]		
	ratio = <b>0.19</b>	> $V_u$	<b>OK</b>	

<b>Bolt Bearing/TearOut Strength on End Plate</b>		ratio = 112.41 / 596.41 = <b>0.19</b>	<b>PASS</b>
<b>Single Bolt Shear Strength</b>			
Bolt shear stress	bolt grade = A325-N	$F_{nv} = 54.0$ [ksi]	AISC 14 <sup>th</sup> Table J3.2
	bolt dia $d_b = 1.250$ [in]	bolt area $A_b = 1.227$ [in <sup>2</sup> ]	
Single bolt shear strength	$R_{n-bolt} = F_{nv} A_b$	= 66.27 [kips]	AISC 14 <sup>th</sup> Eq J3-1
<b>Bolt Bearing/TearOut Strength on Plate</b>			
Bolt hole diameter	bolt dia $d_b = 1\frac{1}{4}$ [in]	bolt hole dia $d_h = 1\frac{5}{16}$ [in]	AISC 14 <sup>th</sup> Table J3.3
Bolt spacing & edge distance	spacing $L_s = 3.346$ [in]	edge distance $L_e = 2.362$ [in]	
Plate tensile strength	$F_u = 65.0$ [ksi]		
Plate thickness	$t = 2.000$ [in]		
<b>Interior Bolt</b>			
Bolt hole edge clear distance	$L_c = L_s - d_h$	= 2.034 [in]	
Bolt tear out/bearing strength	$R_{n-t\&b-in} = 1.5 L_c t F_u \leq 3.0 d_b t F_u$ = 396.53 ≤ 487.50	= 396.53 [kips]	AISC 14 <sup>th</sup> Eq J3-6b
Bolt strength at interior	$R_{n-in} = \min ( R_{n-t\&b-in}, R_{n-bolt} )$	= 66.27 [kips]	
<b>Edge Bolt</b>			
Bolt hole edge clear distance	$L_c = L_e - d_h / 2$	= 1.706 [in]	
Bolt tear out/bearing strength	$R_{n-t\&b-ed} = 1.5 L_c t F_u \leq 3.0 d_b t F_u$ = 332.62 ≤ 487.50	= 332.62 [kips]	AISC 14 <sup>th</sup> Eq J3-6b
Bolt strength at edge	$R_{n-ed} = \min ( R_{n-t\&b-ed}, R_{n-bolt} )$	= 66.27 [kips]	
Number of bolt	interior $n_{in} = 8$	edge $n_{ed} = 4$	
Bolt bearing strength for all bolts	$R_n = n_{in} R_{n-in} + n_{ed} R_{n-ed}$	= 795.22 [kips]	
Required shear strength	$V_u =$	= <b>112.41</b> [kips]	
Bolt resistance factor-LRFD	$\phi = 0.75$		AISC 14 <sup>th</sup> J3-10
	$\phi R_n =$	= <b>596.41</b> [kips]	
	ratio = <b>0.19</b>	> $V_u$	<b>OK</b>

<b>Bolt Bearing/TearOut Strength on Column Flange</b>		ratio = 112.41 / 596.41 = <b>0.19</b>	<b>PASS</b>
<b>Single Bolt Shear Strength</b>			
Bolt shear stress	bolt grade = A325-N	$F_{nv} = 54.0$ [ksi]	AISC 14 <sup>th</sup> Table J3.2
	bolt dia $d_b = 1.250$ [in]	bolt area $A_b = 1.227$ [in <sup>2</sup> ]	
Single bolt shear strength	$R_{n-bolt} = F_{nv} A_b$	= 66.27 [kips]	AISC 14 <sup>th</sup> Eq J3-1
<b>Bolt Bearing/TearOut Strength on Plate</b>			
Bolt hole diameter	bolt dia $d_b = 1\frac{1}{4}$ [in]	bolt hole dia $d_h = 1\frac{5}{16}$ [in]	AISC 14 <sup>th</sup> Table J3.3
Bolt spacing	spacing $L_s = 3.346$ [in]		
Plate tensile strength	$F_u = 65.0$ [ksi]		
Plate thickness	$t = 1.575$ [in]		
<b>Interior Bolt</b>			
Bolt hole edge clear distance	$L_c = L_s - d_h$	= 2.034 [in]	
Bolt tear out/bearing strength	$R_{n-t\&b-in} = 1.5 L_c t F_u \leq 3.0 d_b t m F_u$ = 312.27 ≤ 383.91	= 312.27 [kips]	AISC 14 <sup>th</sup> Eq J3-6b
Bolt strength at interior	$R_{n-in} = \min ( R_{n-t\&b-in}, R_{n-bolt} )$	= 66.27 [kips]	
Number of bolt	interior $n_{in} = 12$		
Bolt bearing strength for all bolts	$R_n = n_{in} R_{n-in}$	= 795.22 [kips]	
Required shear strength	$V_u =$	= <b>112.41</b> [kips]	
Bolt resistance factor-LRFD	$\phi = 0.75$		AISC 14 <sup>th</sup> J3-10
	$\phi R_n =$	= <b>596.41</b> [kips]	
	ratio = <b>0.19</b>	> $V_u$	<b>OK</b>



<b>End Plate Flexural Yielding</b>		ratio = 576.77 / 1894.71 = <b>0.30</b>	<b>PASS</b>
<b>End Plate Bending Strength</b>			
End plate width	$b_{plate} = 16.535$ [in]	thickness $t_p = 2.000$ [in]	
Beam flange width	$b_{fb} = 12.756$ [in]		
Effective end plate width	$b_p = \min ( b_{plate}, b_{fb} + 1" )$	= 13.756 [in]	AISC DG4 Page 9 item 5
End plate yield strength	$F_{yp} = 50.0$ [ksi]		
The following end plate yield line for 12 bolts MRE 1/3-4W/2W bolt pattern is taken from Table 3-12 in Virginia Tech Report to MBMA, Developing and Validating New Bolted End-Plate Moment Connection Configurations July 2015 by Nonish Jain, Matthew Eatherton and Thomas Murray. Thomas Murray is the author of both AISC DG4 and DG16.			
formulas for calculating yield-line parameters			
$s = \frac{1}{2} \sqrt{b_p g}$ use $p_{fi} = s$ when $p_{fi} > s$			
$Y_p = \frac{b_p}{2} \left[ \frac{h_0}{p_{fo}} + \frac{h_1}{p_{fi}} + \frac{h_3}{s} - 1 \right] + \frac{2}{g} \left[ h_1 (p_{fi} + 1.5 p_b) + h_3 (s + 0.5 p_b) \right] + \frac{g}{2}$			
Tension bolt moment arm	$h_0 = 26.043$ [in]	$h_1 = 20.571$ [in]	
	$h_2 = 17.225$ [in]	$h_3 = 13.879$ [in]	
	$g = 5.118$ [in]	$p_b = 3.346$ [in]	
	$p_{fi} = 2.362$ [in]	$p_{fo} = 2.362$ [in]	
	$s = 4.195$ [in]	$Y_p = 245.33$ [in]	
Flexure resistance factor-LRFD	$\phi_b = 0.90$		AISC 14 <sup>th</sup> F1 (1)
End plate bending strength	$\phi_b M_{pl} = \phi_b F_{yp} t_p^2 Y_p$	= <b>3680.00</b> [kip-ft]	
Flange force moment arm	$d_m = d_b - t_{fb}$	= 23.307 [in]	
Flange force required in tension	$P_{uf\_t} = P_u / 2 - M_u / d_m$	= <b>576.77</b> [kips]	
Flange force provided by end plate bending	$\phi R_{pl} = \phi M_{pl} / d_m$	= <b>1894.71</b> [kips]	AISC DG4 Eq 3.10
	ratio = <b>0.30</b>	> $P_{uf\_t}$	<b>OK</b>
<b>End Plate Shear Yielding</b>		ratio = 288.39 / 825.36 = <b>0.35</b>	<b>PASS</b>
Flange force required in tension	$P_{uf\_t} = P_u / 2 - M_u / d_m$	= <b>288.39</b> [kips]	
End plate width	$b_{plate} = 16.535$ [in]	thickness $t_p = 2.000$ [in]	
Beam flange width	$b_{fb} = 12.756$ [in]		
Effective end plate width	$b_p = \min ( b_{plate}, b_{fb} + 1" )$	= 13.756 [in]	AISC DG4 Page 9 item 5
<b>Plate Shear Yielding Check</b>			
Plate size	width $b_p = 13.756$ [in]	thickness $t_p = 2.000$ [in]	
Plate yield strength	$F_y = 50.0$ [ksi]		
Plate gross area in shear	$A_{gv} = b_p t_p$	= 27.512 [in <sup>2</sup> ]	
Shear force required	$0.5 P_{uf\_t} =$	= <b>288.39</b> [kips]	
Plate shear yielding strength	$R_n = 0.6 F_y A_{gv}$	= 825.36 [kips]	AISC 14 <sup>th</sup> Eq J4-3
Resistance factor-LRFD	$\phi = 1.00$		AISC 14 <sup>th</sup> Eq J4-3
	$\phi R_n =$	= <b>825.36</b> [kips]	
	ratio = <b>0.35</b>	> $0.5 P_{uf\_t}$	<b>OK</b>

<b>End Plate Shear Rupture</b>		ratio = 288.39 / 643.85 = <b>0.45</b> <b>PASS</b>	
Flange force required in tension	$P_{uf,t} = P_u / 2 - M_u / d_m$	= <b>288.39</b> [kips]	
End plate width	$b_{plate} = 16.535$ [in]	thickness $t_p = 2.000$	[in]
Beam flange width	$b_{fb} = 12.756$ [in]		
Effective end plate width	$b_p = \min ( b_{plate}, b_{fb} + 1" )$	= 13.756 [in]	AISC DG4 Page 9 item 5
<b>Plate Shear Rupture Check</b>			
Bolt hole diameter	bolt dia $d_b = 1\frac{1}{4}$ [in]	bolt hole dia $d_h = 1\frac{3}{8}$ [in]	AISC 14 <sup>th</sup> B4.3b
Number of bolt	$n = 2$		
Plate size	width $b_p = 13.756$ [in]	thickness $t_p = 2.000$	[in]
Plate tensile strength	$F_u = 65.0$ [ksi]		
Plate net area in shear	$A_{nv} = ( b_p - n d_h ) t_p$	= 22.012 [in <sup>2</sup> ]	
Shear force required	$0.5 P_{uf,t} =$	= <b>288.39</b> [kips]	
Plate shear rupture strength	$R_n = 0.6 F_u A_{nv}$	= 858.47 [kips]	AISC 14 <sup>th</sup> Eq J4-4
Resistance factor-LRFD	$\phi = 0.75$	AISC 14 <sup>th</sup> Eq J4-4	
	$\phi R_n =$	= <b>643.85</b> [kips]	
	ratio = <b>0.45</b>	> 0.5 $P_{uf,t}$	<b>OK</b>

<b>Beam Web Weld Strength</b>		ratio = 112.41 / 152.30 = <b>0.74</b>		<b>PASS</b>
<b>Beam Web Effective Weld Length Calc</b>				
Beam section	$d_b = 24.055$ [in]	$t_{fb} = 0.748$ [in]		
	$k_b = 1.614$ [in]			
Bolt diameter	$d_{bolt} = 1.250$ [in]	bolt inner pitch $p_{fi} = 2.362$ [in]		
Effective weld length case 1	$L_1 = 0.5 d_b - k_b$	$= 10.414$ [in]		AISC DG4 Page 38
Effective weld length case 2	$L_2 = d_b - 2t_{fb} - p_{fi} - 2 d_{bolt}$	$= 17.697$ [in]		AISC DG4 Page 38
Fillet weld length - double fillet	$L = \min(L_1, L_2)$	$= \mathbf{10.414}$ [in]		
<b>Fillet Weld Strength Check</b>				
Fillet weld leg size	$w = \frac{3}{8}$ [in]	load angle $\theta = 0.0$ [°]		
Electrode strength	$F_{EXX} = 70.0$ [ksi]	strength coeff $C_1 = 1.00$		AISC 14 <sup>th</sup> Table 8-3
Number of weld line	$n = 2$ for double fillet			
Load angle coefficient	$C_2 = (1 + 0.5 \sin^{1.5} \theta)$	$= 1.00$		AISC 14 <sup>th</sup> Page 8-9
Fillet weld shear strength	$R_{n-w} = 0.6 (C_1 \times 70 \text{ ksi}) 0.707 w n C_2$	$= 23.381$ [kip/in]		AISC 14 <sup>th</sup> Eq 8-1
Base metal - beam web	thickness $t = 0.500$ [in]	tensile $F_u = 65.0$ [ksi]		
Base metal - beam web is in shear, <u>shear</u> rupture as per AISC 14 <sup>th</sup> Eq J4-4 is checked				AISC 14 <sup>th</sup> J2.4
Base metal shear rupture	$R_{n-b} = 0.6 F_u t$	$= 19.500$ [kip/in]		AISC 14 <sup>th</sup> Eq J4-4
Double fillet linear shear strength	$R_n = \min(R_{n-w}, R_{n-b})$	$= \mathbf{19.500}$ [kip/in]		AISC 14 <sup>th</sup> Eq 9-2
Resistance factor-LRFD	$\phi = 0.75$			AISC 14 <sup>th</sup> Eq 8-1
	$\phi R_n =$	$= \mathbf{14.625}$ [kip/in]		
Shear resistance required	$V_u =$	$= \mathbf{112.41}$ [kips]		
Fillet weld length - double fillet	$L =$	$= 10.414$ [in]		
Shear resistance provided	$\phi F_n = \phi R_n \times L$	$= \mathbf{152.30}$ [kips]		
	ratio = <b>0.74</b>	$> V_u$	<b>OK</b>	

**Column Flexural Yielding**ratio = 576.77 / 2099.72 = **0.27** **PASS****Column Flange Bending Strength**

The column flange yield line for MRE 1/3 bolt pattern is taken from Table 8.13 of Virginia Tech Emmet Sumner's PhD thesis - Unified Design of Extended End-Plate Moment Connections Subject to Cyclic Loading June, 2003. This thesis was approved by Thomas M. Murray who is the author of AISC DG4 and DG16.

formulas for calculating yield-line parameters

$$s = \frac{1}{2} \sqrt{b_{fc} g}$$

$$Y_c = \frac{b_{fc}}{2} \left[ \frac{h_1}{p_{si}} + \frac{h_3}{s} + h_0 \left( \frac{1}{p_{so}} + \frac{1}{s} \right) \right] + \frac{2}{g} \left[ h_1 \left( p_{si} + \frac{3}{2} p_b \right) + h_3 \left( s + \frac{p_b}{2} \right) + h_0 (p_{so} + s) \right] + \frac{g}{2}$$

Tension bolt moment arm

 $h_0 = 26.043$  [in] $h_1 = 20.571$  [in] $h_2 = 17.225$  [in] $h_3 = 13.879$  [in]

\*\*\* Stiffened Column Flange Case \*\*\*

Column section

 $b_{fc} = 19.685$  [in] $t_{fc} = 1.575$  [in] $F_{yc} = 50.0$  [ksi] $g = 5.118$  [in] $s = 5.019$  [in] $c = 5.472$  [in]

Stiffener plate thickness

 $t_s = 0.500$  [in] $p_{si} = 2.486$  [in] $p_{so} = 2.486$  [in] $p_b = 3.346$  [in] $Y_c = 438.4$  [in]

Flexure resistance factor-LRFD

 $\phi_b = 0.90$ AISC 14<sup>th</sup> F1 (1)

Column flange bending strength

 $\phi_b M_{cf} = \phi_b F_{yc} t_{fc}^2 Y_c$ = **4078.19** [kip-ft]

Flange force moment arm

 $d_m = d_b - t_{fb}$ 

= 23.307 [in]

Flange force required in tension

 $P_{uf,t} = P_u / 2 - M_u / d_m$ = **576.77** [kips]

Flange force provided by column

 $\phi R_{cf} = \phi M_{cf} / d_m$ = **2099.72** [kips]

AISC DG4 Eq 3.21

flange bending

ratio = **0.27**>  $P_{uf,t}$  **OK**

<b>Column Web Yielding</b>		ratio = 576.77 / 975.85 = <b>0.59</b>		<b>PASS</b>
Column web thickness	$t_{wc} = 0.787$ [in]	yield $F_y = 50.0$ [ksi]		
Doubler plate thickness	$t_{dp} = 0.375$ [in]	yield $F_{ydp} = 50.0$ [ksi]		
Equivalent web thickness when considering doubler plate	$t_{w-eq} = t_{wc} + t_{dp} \times F_{ydp} / F_y$	= 1.162 [in]		
Flange force moment arm	$d_m = d_b - t_{fb}$	= 23.307 [in]		
Flange force in demand	$P_{uf} = \max ( P_{uf_t}, P_{uf_c} )$	= <b>576.77</b> [kips]		AISC DG13 Eq 4.2-1
Column section	$d_c = 19.685$ [in]	$t_{fc} = 1.575$ [in]		
	$t_{wc} = 0.787$ [in]	$k_c = 2.008$ [in]		
Column yield strength	$F_{yc} = 50.0$ [ksi]			
Top column condition	it's not a top column case	$C_t = 1.0$		AISC DG4 Eq 3.24
Beam flange fillet weld size	$w = 0.000$ [in]	beam flange $t_{fb} = 0.748$ [in]		
Length of bearing	$N = t_{fb} + 2 w$	= 0.748 [in]		AISC DG4 Eq 3.24
End plate thickness	$t_p = 2.000$ [in]			
Column web yielding strength	$R_n = C_t ( 6 k_c + N + 2 t_p ) F_{yc} t_{w-eq}$	= 975.85 [kips]		AISC DG4 Eq 3.24
Resistance factor-LRFD	$\phi = 1.00$			AISC 14 <sup>th</sup> J10.2
	$\phi R_n =$	= <b>975.85</b> [kips]		
	ratio = <b>0.59</b>	> $P_{uf}$	<b>OK</b>	
<b>Column Web Buckling</b>		ratio = 509.32 / 896.67 = <b>0.57</b>		<b>PASS</b>
Flange force moment arm	$d_m = d_b - t_{fb}$	= 23.307 [in]		
Flange force required in compression	$P_{uf_c} = P_u / 2 - M_u / d_m$	= <b>509.32</b> [kips]		
Column section	$d_c = 19.685$ [in]	$t_{fc} = 1.575$ [in]		
	$t_{wc} = 0.787$ [in]	$k_c = 2.008$ [in]		
	$h = d_c - 2 k_c$	= 15.669 [in]		
Column yield strength	$F_{yc} = 50.0$ [ksi]	$E_c = 29000$ [ksi]		
Top column condition	it's not a top column case	$C_t = 1.0$		AISC 14 <sup>th</sup> J10.5
Column web buckling strength	$R_{n1} = \frac{C_t 24 t_{wc}^3 \sqrt{E_c F_{yc}}}{h}$	= 899.04 [kips]		AISC 14 <sup>th</sup> Eq J10-8
Doubler plate thickness	$t_{dp} = 0.375$ [in]	yield $F_{ydp} = 50.0$ [ksi]		
Doubler plate buckling strength	$R_{n2} = \frac{C_t 24 t_{dp}^3 \sqrt{E_c F_{ydp}}}{h}$	= 97.26 [kips]		AISC 14 <sup>th</sup> Eq J10-8
Total buckling strength	$R_n = R_{n1} + R_{n2}$	= 996.30 [kips]		
Resistance factor-LRFD	$\phi = 0.90$			AISC 14 <sup>th</sup> J10.5
	$\phi R_n =$	= <b>896.67</b> [kips]		
	ratio = <b>0.57</b>	> $P_{uf_c}$	<b>OK</b>	

<b>Column Web Crippling</b>		ratio = 509.32 / 1020.57 = <b>0.50</b>	<b>PASS</b>
Flange force moment arm	$d_m = d_b - t_{fb}$	= 23.307 [in]	
Flange force required in compression	$P_{uf\_c} = P_u / 2 - M_u / d_m$	= <b>509.32</b> [kips]	
Column section	$d_c = 19.685$ [in]	$t_{fc} = 1.575$ [in]	
	$t_{wc} = 0.787$ [in]	$k_c = 2.008$ [in]	
Column yield strength	$F_{yc} = 50.0$ [ksi]	$E_c = 29000$ [ksi]	
Beam flange fillet weld size	$w = 0.000$ [in]	beam flange $t_{fb} = 0.748$ [in]	
End plate thickness	$t_p = 2.000$ [in]		
Length of bearing	$l_b = t_{fb} + 2 w + 2 t_p$	= 4.748 [in]	
Distance from top of column to top of beam flange	$d_{end-flg} =$	= 0.374 [in]	
Top column condition	it's not a top column case, use Eq J10-4		AISC 14 <sup>th</sup> J10.3 (a)
Column web crippling strength	$R_{n1} = 0.8 t_{wc}^2 [1 + 3 \frac{l_b}{d_c} (\frac{t_{wc}}{t_{fc}})^{1.5}] \times (\frac{E_c F_{yc} t_{fc}}{t_{wc}})^{0.5}$	= 1059.80 [kips]	AISC 14 <sup>th</sup> Eq J10-4
Doubler plate thickness	$t_{dp} = 0.375$ [in]	yield $F_{ydp} = 50.0$ [ksi]	
Doubler plate crippling strength	$R_{n2} = 0.8 t_{dp}^2 [1 + 3 \frac{l_b}{d_c} (\frac{t_{dp}}{t_{fc}})^{1.5}] \times (\frac{E_c F_{ydp} t_{fc}}{t_{dp}})^{0.5}$	= 300.97 [kips]	AISC 14 <sup>th</sup> Eq J10-4
Total crippling strength	$R_n = R_{n1} + R_{n2}$	= 1360.76 [kips]	
Resistance factor-LRFD	$\phi = 0.75$		AISC 14 <sup>th</sup> J10.3
	$\phi R_n =$	= <b>1020.57</b> [kips]	
	ratio = <b>0.50</b>	> $P_{uf\_c}$	<b>OK</b>
<b>Column Panel Zone Shear</b>		509.32 / 418.29	<b>N/A</b>
Panel zone shear force	$V_p = P_{f\_TR} - P_{f\_TL} - V_s$	= <b>509.32</b> [kips]	
Column section	$d_c = 19.685$ [in]	$t_{wc} = 0.787$ [in]	
	$A_c = 75.330$ [in <sup>2</sup> ]	$F_{yc} = 50.0$ [ksi]	
Column axial compression - user input	$P_r =$	= 0.00 [kips]	
	$P_c = P_y = F_{yc} A_c$	= 3766.50 [kips]	AISC 14 <sup>th</sup> J10.6
	$P_r \leq 0.4 P_c$ , use Eq J10-9		AISC 14 <sup>th</sup> Eq J10-9
Web panel zone capacity	$R_n = 0.6 F_{yc} d_c t_{wc}$	= 464.76 [kips]	AISC 14 <sup>th</sup> Eq J10-9
Resistance factor-LRFD	$\phi = 0.90$		AISC 14 <sup>th</sup> J10.6
	$\phi R_n =$	= <b>418.29</b> [kips]	
Unbalanced force to be resisted by doubler plate	$V_{dp} = R_p - \phi R_n$	= <b>91.03</b> [kips]	

<b>Doubler Geometry Restriction</b>		<b>PASS</b>	
<b>Min Doubler Thickness to Allow for Proper Beveling of Plate</b>		AISC DG13 Eq 4.4-4	
Column section	$t_{fc} = 1.575$ [in]	$k_c = 2.008$ [in]	
Allowed fillet encroachment	$r_e = 0.188$ [in]		AISC 14 <sup>th</sup> Fig 10-3
Min doubler plate thickness	$t_{pmin} = k_c - t_{fc} - r_e$	<b>= 0.245</b> [in]	AISC DG13 Eq 4.4-4
Doubler plate thickness	$t_{dp} =$	<b>= 0.375</b> [in]	
		<b>&gt; <math>t_{pmin}</math></b>	<b>OK</b>
<b>Min Doubler Thickness to Avoid Shear Buckling of Plate</b>		AISC DG13 Eq 4.4-5	
Column section	$d_c = 19.685$ [in]	$k_c = 2.008$ [in]	
	$h = d_c - 2 k_c$	<b>= 15.669</b> [in]	
Doubler plate steel	$F_y = 50.0$ [ksi]	$E = 29000$ [ksi]	
Min doubler plate thickness	$t_{pmin} = h / 2.24 \sqrt{E / F_y}$	<b>= 0.290</b> [in]	AISC 14 <sup>th</sup> G2.1 (a)
Doubler plate thickness	$t_{dp} =$	<b>= 0.375</b> [in]	
		<b>&gt; <math>t_{pmin}</math></b>	<b>OK</b>
<b>Doubler Plate Shear Yield</b>		ratio = 91.03 / 221.46	<b>= 0.41 PASS</b>
Doubler plate thickness	$t_{dp} = 0.375$ [in]	yield strength $F_y = 50.0$ [ksi]	
Number of doubler	$N_{dbl} = 1$ for one side		
Column depth	$d_c = 19.685$ [in]		
Area of web	$A_w = t_{dp} \times d_c$	<b>= 7.382</b> [in <sup>2</sup> ]	AISC DG13 Eq 4.4-1
Shear coefficient	$C_v = 1.0$		AISC 14 <sup>th</sup> Eq G2-2
Doubler plate shear in demand	$R_{dp} =$ unbalanced force from column panel zone shear calc	<b>= 91.03</b> [kips]	
Doubler plate shear strength	$R_n = N_{dbl} 0.6 F_y A_w C_v$	<b>= 221.46</b> [kips]	AISC 14 <sup>th</sup> Eq G2-1
Resistance factor-LRFD	$\phi = 1.00$		AISC 14 <sup>th</sup> G2.1 (a)
	$\phi R_n =$	<b>= 221.46</b> [kips]	
	ratio = <b>0.41</b>	<b>&gt; <math>R_{dp}</math></b>	<b>OK</b>
<b>Doubler to Column Flange Fillet Weld Limitation</b>		<b>PASS</b>	
<b>Min Fillet Weld Size</b>			
Thinner part joined thickness	$t =$	<b>= 0.375</b> [in]	
Min fillet weld size allowed	$w_{min} =$	<b>= 0.188</b> [in]	AISC 14 <sup>th</sup> Table J2.4
Fillet weld size provided	$w =$	<b>= 0.315</b> [in]	
		<b>&gt; <math>w_{min}</math></b>	<b>OK</b>
<b>Min Fillet Weld Length</b>			
Fillet weld size provided	$w =$	<b>= 0.315</b> [in]	
Min fillet weld length allowed	$L_{min} = 4 \times w$	<b>= 1.260</b> [in]	AISC 14 <sup>th</sup> J2.2b
Min fillet weld length	$L = d_b + (3 k_c + t_p) \times 2$ Ends	<b>= 40.103</b> [in]	
		<b>&gt; <math>L_{min}</math></b>	<b>OK</b>

Doubler to Column Web Fillet Weld Limitation		PASS	
<b>Min Fillet Weld Size</b>			
Thinner part joined thickness	$t =$	$= 0.375$ [in]	
Min fillet weld size allowed	$w_{min} =$	$= 0.188$ [in]	AISC 14 <sup>th</sup> Table J2.4
Fillet weld size provided	$w =$	$= 0.315$ [in]	
		$> w_{min}$	OK
<b>Min Fillet Weld Length</b>			
Fillet weld size provided	$w =$	$= 0.315$ [in]	
Min fillet weld length allowed	$L_{min} = 4 \times w$	$= 1.260$ [in]	AISC 14 <sup>th</sup> J2.2b
Min fillet weld length	$L = d_c - 2 \times k_c$	$= 15.669$ [in]	
		$> L_{min}$	OK
<b>Doubler Weld Strength at Column Flange</b>		ratio = 91.03 / 281.30 = 0.32	PASS
<b>Doubler Plate to Column Flange Weld Length Calc</b>			
Beam section	$d_b = 24.055$ [in]	column section $k_c = 2.008$ [in]	
End plate thickness	$t_p = 2.000$ [in]		
Doubler plate to column flange weld length - single fillet	$L = d_b + (3 k_c + t_p) \times 2 \text{ ends}$	$= 40.103$ [in]	AISC DG13 Fig 4-3
<b>Fillet Weld Strength Check</b>			
Fillet weld leg size	$w = 5/16$ [in]	load angle $\theta = 0.0$ [°]	
Electrode strength	$F_{EXX} = 70.0$ [ksi]	strength coeff $C_1 = 1.00$	AISC 14 <sup>th</sup> Table 8-3
Number of weld line	$n = 1$ for single fillet		
Load angle coefficient	$C_2 = (1 + 0.5 \sin^{1.5} \theta)$	$= 1.00$	AISC 14 <sup>th</sup> Page 8-9
Fillet weld shear strength	$R_{n-w} = 0.6 (C_1 \times 70 \text{ ksi}) 0.707 w n C_2$	$= 9.352$ [kip/in]	AISC 14 <sup>th</sup> Eq 8-1
Base metal - doubler plate	thickness $t = 0.375$ [in]	tensile $F_u = 65.0$ [ksi]	
Base metal - doubler plate is in shear, shear rupture as per AISC 14 <sup>th</sup> Eq J4-4 is checked			AISC 14 <sup>th</sup> J2.4
Base metal shear rupture	$R_{n-b} = 0.6 F_u t$	$= 14.625$ [kip/in]	AISC 14 <sup>th</sup> Eq J4-4
Single fillet linear shear strength	$R_n = \min (R_{n-w}, R_{n-b})$	$= 9.352$ [kip/in]	AISC 14 <sup>th</sup> Eq 9-2
Resistance factor-LRFD	$\phi = 0.75$		AISC 14 <sup>th</sup> Eq 8-1
	$\phi R_n =$	$= 7.014$ [kip/in]	
Shear resistance required	$R_{dp} =$	$= 91.03$ [kips]	
Fillet weld length - single fillet	$L =$	$= 40.103$ [in]	
Shear resistance provided	$\phi F_n = \phi R_n \times L$	$= 281.30$ [kips]	
	ratio = 0.32	$> R_{dp}$	OK



<b>Doubler Weld Strength at Column Web</b>		ratio = 91.03 / 109.91	= <b>0.83</b>	<b>PASS</b>
<b>Doubler Plate to Column Web Weld Length Calc</b>				
Column section	$d_c = 19.685$ [in]	$k_c = 2.008$ [in]		
Doubler plate to column web weld length - single fillet	$L = d_c - 2 \times k_c$		= <b>15.669</b> [in]	
<b>Fillet Weld Strength Check</b>				
Fillet weld leg size	$w = 5/16$ [in]	load angle $\theta = 0.0$ [°]		
Electrode strength	$F_{EXX} = 70.0$ [ksi]	strength coeff $C_1 = 1.00$		AISC 14 <sup>th</sup> Table 8-3
Number of weld line	$n = 1$ for single fillet			
Load angle coefficient	$C_2 = (1 + 0.5 \sin^{1.5} \theta)$	= 1.00		AISC 14 <sup>th</sup> Page 8-9
Fillet weld shear strength	$R_{n-w} = 0.6 (C_1 \times 70 \text{ ksi}) 0.707 w n C_2$	= 9.352 [kip/in]		AISC 14 <sup>th</sup> Eq 8-1
Base metal - doubler plate thickness $t = 0.375$ [in]		tensile $F_u = 65.0$ [ksi]		
Base metal - doubler plate is in shear, <u>shear</u> rupture as per AISC 14 <sup>th</sup> Eq J4-4 is checked				AISC 14 <sup>th</sup> J2.4
Base metal shear rupture	$R_{n-b} = 0.6 F_u t$	= 14.625 [kip/in]		AISC 14 <sup>th</sup> Eq J4-4
Single fillet linear shear strength	$R_n = \min (R_{n-w}, R_{n-b})$	= <b>9.352</b> [kip/in]		AISC 14 <sup>th</sup> Eq 9-2
Resistance factor-LRFD	$\phi = 0.75$			AISC 14 <sup>th</sup> Eq 8-1
	$\phi R_n =$	= <b>7.014</b> [kip/in]		
Shear resistance required	$R_{dp} =$	= <b>91.03</b> [kips]		
Fillet weld length - single fillet	$L =$	= 15.669 [in]		
Shear resistance provided	$\phi F_n = \phi R_n \times L$	= <b>109.91</b> [kips]		
	ratio = <b>0.83</b>	> $R_{dp}$	<b>OK</b>	